Leveraging Quantum Annealing for Large MIMO Processing in Centralized Radio Access Networks

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ABSTRACT

User demand for increasing amounts of wireless capacity continues to outpace supply, and so to meet this demand, significant progress has been made in new MIMO wireless physical layer techniques. Higher-performance systems now remain impractical largely only because their algorithms are extremely computationally demanding. For optimal performance, an amount of computation that increases at an exponential rate both with the number of users and with the data rate of each user is often required. The base station’s computational capacity is thus becoming one of the key limiting factors on wireless capacity. QuAMax is the first large MIMO centralized radio access network design to address this issue by leveraging quantum annealing on the problem. We have implemented QuAMax on the 2,031 qubit D-Wave 2000Q quantum annealer, the state-of-the-art in the field. Our experimental results evaluate that implementation on real and synthetic MIMO channel traces, showing that 10 µs of compute time on the 2000Q can enable 48 user, 48 AP antenna BPSK communication at 20 dB SNR with a bit error rate of 10^{-6} and a 1,500 byte frame error rate of 10^{-4}.

CCS CONCEPTS

- Networks → Wireless access points, base stations and infrastructure;  
- Hardware → Quantum computation;

KEYWORDS

Wireless Networks, Massive MIMO, Maximum Likelihood Detection, Sphere Decoder, Quantum Computing, Quantum Annealing

ACM Reference Format:


1 INTRODUCTION

A central design challenge for future generations of wireless networks is to meet users’ ever-increasing demand for capacity and throughput. Recent advances in the design of wireless networks to this end, including the 5G efforts underway in industry and academia, call in particular for the use of Large and Massive multiple input multiple output (MIMO) antenna arrays to support many users near a wireless access point (AP) or base station sharing the wireless medium at the same time.1

Much effort has been and is currently being dedicated to large and massive MIMO, and these techniques are coming to fruition, yielding significant gains in network throughput. An apropos example is Massive MIMO: in LTE cellular and 802.11ac local-area networks, up to eight antennas are supported at the AP spatially multiplexing [65] parallel information streams concurrently to multiple receive antennas. The technique is also known as multi-user MIMO (MU-MIMO) and can be used both in the uplink and the downlink of multi-user MIMO networks: in the uplink case, several users concurrently transmit to a multi-antenna AP, while over the downlink, the AP multiplexes different information streams to a number of mobile users.

From a design standpoint, one of the most promising and cost effective architectures to implement 5G technologies is the centralized radio access network (C-RAN) architecture [48, 60]. C-RAN pushes most of the physical-layer processing that currently takes place at the AP to a centralized data center, where it is aggregated with other APs’ processing on the same hardware. The C-RAN concept has undergone several iterations since its inception, with more recent work treating the unique demands of small cells [63], centralizing most of the computing and supporting hundreds or thousands of the APs from a centralized data center.

To fully realize Massive MIMO’s potential throughput gains, however, the system must effectively and efficiently demultiplex mutually-interfering information streams as they arrive. Current large MIMO designs such as Argos [62], BigStation [76], and SAM [64] use linear processing methods such as zero-forcing and minimum mean squared error (MMSE) filters. These methods have the advantage of very low computational complexity, but suffer when the MIMO channel is poorly-conditioned [50], as is often the case when the number of user antennas approaches the number of antennas at the AP [50, 76]. Sphere Decoder-based maximum likelihood (ML) MIMO decoders/detectors [10, 50] can significantly improve throughput over such linear filters, but suffer from increased computational complexity: compute requirements increase exponentially with the number of antennas [50], soon becoming prohibitive (Section 2.1).

The problem of limited computational capacity stems from the requirement that a receiver’s physical layer finish decoding a frame before the sender requires feedback about its decoding success or failure. For Wi-Fi networks, e.g., this quantity is on the order of

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1We use the terms “access point” and “base station” interchangeably in this paper.
tens of μs, the spacing in time between the data frame and its acknowledgement. More sophisticated physical layers, such as 4G LTE, require the receiver to give feedback in the context of incremental redundancy schemes, for the same reason; the processing time available is 3 ms for 4G LTE and 10 ms for WCDMA [19, 76]. As a result, most current systems adopt linear filters, accepting a drop in performance.

New approach: Quantum computation in the data center. This paper explores the leveraging of quantum computation (QC) to speed up the computation required for the ML MIMO decoder. We place our ideas in the context of the QC currently already realized in experimental hardware, and in the context of the dominant C-RAN architecture. Here we imagine a future quantum computer, co-located with C-RAN computational resources in a data center, connected to the APs via high-speed, low-latency fiber or millimeter-wave links.

Optimization is one of the key applications the quantum community has identified as viable in the short-term (i.e. before quantum processors become scalable devices capable of error correction and universality). While their potential in optimization is largely unproven, it is believed that it may be possible for Noisy Intermediate-Scale Quantum (NISQ) devices to achieve polynomial or exponential speedups over the best known classical algorithms [56]. It is, however, important to leverage understanding from current prototypes in order to inform the design of real-world systems, since performance cannot be predicted or simulated efficiently, especially in the presence of device-specific noise. This is the approach we therefore advocate here. Two main approaches have been identified for quantum optimization in NISQs: Quantum Annealing (QA) and Quantum Approximate Optimization Algorithms (QAOA). The former approach is a form of analog computation that has been developed theoretically in the early nineties [25], but realized experimentally in a programmable device only in 2011 by D-Wave Systems. We focus on QA here, discussing QAOA briefly in Section 6.

This paper presents QuAMax, the first system to apply QA to the computationally challenging ML MIMO wireless decoding problem in the context of a centralized RAN architecture where a QA is co-located in a data center serving one or more wireless APs. The contributions of our paper can be summarized as follows: Firstly, we present the first reduction of the ML MIMO wireless decoding problem to a form that a QA solver can process. Secondly, we introduce a new, communications-specific evaluation metric, Time-to-BER (TTB), which evaluates the performance of the QA as it aims to achieve a target bit error rate (BER) on the decoded data. Finally, we evaluate QuAMax with various scenarios and parameter settings and test their impact on computational performance. To achieve a BER of \(10^{-6}\) and a frame error rate of \(10^{-4}\), ML MIMO detection on the D-Wave 2000Q quantum annealer requires 10–20 μs of computation time for 48-user, 48-AP antenna binary modulation or 30–40 μs for 14 × 14 QPSK at 20 dB SNR, and with the real-world trace of \(8 \times 8\) MIMO channel, the largest spatial multiplexing MIMO size publicly available for experiments [61], QuAMax requires 2 μs for BPSK and 2–10 μs for QPSK.

### Paper roadmap

The next section is a background primer on ML detection and QA. Section 3 details our programming of the ML problem on the QA hardware. Section 4 describes QuAMax implementation in further detail, followed by our evaluation in Section 5. We conclude with a review of related work (Section 6), discussion of current status of technology and practical considerations (Section 7), and final considerations (Section 8).

### 2 BACKGROUND

In this section, we present primer material on the MIMO ML Detection problem (§2.1), and Quantum Annealing (§2.2).

#### 2.1 Primer: Maximum Likelihood Detection

Suppose there are \(N_t\) mobile users, each of which has one antenna, each sending data bits to a multi-antenna \((N_r \geq N_t)\) MIMO AP based on OFDM, the dominant physical layer technique in broadband wireless communication systems [49]. Considering all users’ data bits together in a vector whose elements each comprise a single user’s data bits, the users first map those data bits into a complex-valued symbol \(\bar{v}\) that is transmitted over a radio channel: 
\[
\bar{v} = [\bar{v}_1, \bar{v}_2, \ldots, \bar{v}_N]^\top \in \mathbb{C}^{N_t}.
\]
Each user sends from a constellation \(O\) of size \(|O| = 2^Q\) (Q bits per symbol). The MIMO decoding problem, whose optimal solution is called the ML solution, consisting of a search over the sets of transmitted symbols, looking for the set that minimizes the error with respect to what has been received at the AP:
\[
\hat{v} = \arg \min_{v \in O^{N_t}} \|y - Hv\|^2. \tag{1}
\]

The ML detector then “de-maps” the decoded symbols \(\hat{v}\) to decoded bits \(\tilde{b}\). In Eq. 1, \(H \in \mathbb{C}^{N_r \times N_t} = H^H + jH^Q\) is the wireless channel on each OFDM subcarrier and \(y \in \mathbb{C}^{N_r} = (HS + n)\) is the received set of symbols, perturbed by \(n \in \mathbb{C}^{N_r}\), additive white Gaussian noise (AWGN). This solution minimizes detection errors, thus maximizing throughput (i.e., throughput-optimal decoding).

The Sphere Decoder [1, 20] is a ML detector that reduces complexity with respect to brute-force search by constraining its search to only possible sets \(v\) that lie within a hypersphere of radius \(\sqrt{C}\) centered around \(y\) (i.e., Eq. 1 with constraint \(\|y - Hv\|^2 \leq C\)). It transforms Eq. 1 into a tree search [71] by QR decomposition \(H = QR\), where \(Q\) is orthonormal and \(R\) upper-triangular, resulting in \(\hat{v} = \arg \min_{v \in O^{N_t}} \|y - Rv\|^2\), with \(y = Q^\top y\). The resulting tree has a height of \(N_t\), branching factor of \(|O|,\) and \(1 + \sum_{i=1}^{N_t} |O|^i\) nodes. ML detection becomes the problem of finding the single leaf among \(|O|^{N_t}\) with minimum metric; the corresponding tree path is the

#### Table 1: Sphere Decoder visited node count [30], complexity over 10,000 instances, and practicality on a Skylake Core i7 architecture.

<table>
<thead>
<tr>
<th>BPSK</th>
<th>QPSK</th>
<th>16-QAM</th>
<th>Complexity (Visited Nodes)</th>
</tr>
</thead>
<tbody>
<tr>
<td>12 × 12</td>
<td>7 × 7</td>
<td>4 × 4</td>
<td>≈ 40 (feasible)</td>
</tr>
<tr>
<td>21 × 21</td>
<td>11 × 11</td>
<td>6 × 6</td>
<td>≈ 270 (borderline)</td>
</tr>
<tr>
<td>30 × 30</td>
<td>15 × 15</td>
<td>8 × 8</td>
<td>≈ 1,900 (unfeasible)</td>
</tr>
</tbody>
</table>

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\(\text{The channel changes every channel coherence time, and is practically estimated and tracked via preamble and/or pilot tones. Typical coherence time at 2 GHz and a walking speed is ca. 30 ms [67].}\)
ML solution. Thus, the min in Eq. 1 is a search in an exponentially-large space of transmitted symbols \( \{v\} \), despite Sphere Decoder reductions in the search space size [71].

Table 1 shows the average number of tree nodes visited to perform ML Sphere decoding, with clients transmitting modulation symbols on 50 subcarriers over a 20 MHz, 13 dB SNR (Signal to Noise Ratio) Rayleigh channel. The table is parameterized on the number of clients and AP antennas, and the modulation, highlighting the exponential increase in computation. For 8 clients with 16-QAM symbols, 15 clients with QPSK symbols, or 30 clients sending binary (BPSK) symbols, the Sphere Decoder visits close to 2,000 tree nodes, saturating, for example, Intel’s Skylake core i7 architecture, whose arithmetic subsystem achieves an order of magnitude less computational throughput [32]. Since traditional silicon’s clock speed is plateauing [14], the problem is especially acute.

### 2.2 Primer: Quantum Annealing

Quantum Annealers [37, 45] are specialized, analog computers that solve NP-complete and NP-hard optimization problems on current hardware, with future potential for substantial speedups over conventional computing [46]. Many NP-hard problems can be formulated in the Ising model [42] (cf. §3.2), which many QA machines use as input [6, 18]. NP-complete and NP-hard problems other than ML MIMO detection in the field of (wireless) networking that potentially benefit from QA include MIMO downlink precoding [44], channel coding [36, 75], network routing [11], security [26], and scheduling [27, 41].

**Quantum Annealing hardware.** Compared to simulated annealing, the classical algorithm from which QA inherits its name, QA aims to exploit quantum effects such as tunneling, many-body de-localization and quantum relaxation to circumvent computational bottlenecks that would otherwise trap Monte Carlo methods in local minima of the solution landscape. While exploiting QA is technologically challenging, with the appearance of the D-Wave quantum annealer (Fig. 1), the research community is now able to run experiments, and critically, to study under what conditions a noisy-intermediate-scale-quantum (NISQ) machine [56] can use quantum resources to deliver a speedup [34]. For instance, recently Boixo et al. [5] and Denchev et al. [22] have found evidence that tunneling under ideal conditions can be exploited on an earlier model of the D-Wave 2000Q (DW2Q) machine, delivering many orders of magnitude speedup against CPU-based simulated annealing, which is considered to be one of the best classical competitions to Quantum Processing Units (QPUs). QPUs also outperform GPU implementations by several orders of magnitude in random problems whose structure is related to real world optimization problems [38].

The DW2Q is an analog optimizer, meaning that it computes continuously rather than in discrete clock cycles, and that it represents numerical quantities as analog instead of digital quantities. The hardware initializes each of its \( N \) constituent *quantum bits*, or *qubits*, to begin in a *superposition state* \( \frac{1}{\sqrt{2}} (|0\rangle + |1\rangle) \) that has no classical counterpart. In concrete terms, these qubits are metallic circuits in a chip that are maintained in a superconducting state by low temperature and subjected to the influence of tailored magnetic fluxes. The collection of \( N \) qubits at this point in time encodes all the possible \( 2^N \) outputs in a single state. This initial setting is achieved by exposing all the qubits in the chip to a signal \( A(t) \) whose magnitude at this point in time is maximal. Then the system implements an *objective function* which is represented by another signal \( B(t) \) and is ramped up from zero, while \( A(t) \) is decreased progressively at the same time. The synchronized sequence of signals \( A \) and \( B \) and their time dependence is the *annealing schedule*. The schedule is essentially the QA algorithm, and has to be optimized so that at the end of the run \( B(t) = \text{max} \) and \( A(t) = 0 \), each qubit in the chip assumes either a value of \( 0 \) or \( 1 \), corresponding to classical bit values, 0 or 1, respectively. This final state of these qubits collectively represents a candidate solution of the problem, ideally the *ground state* of the system (i.e., the minimum of the optimization objective function) [24, 35].

In practice, at the end of the run, the ground state will be found with a probability that depends on the degree to which the schedule is optimal for the problem at hand, as well as on the effect of uncontrollable QA noise and environmental interference on the annealer. While the quantum community is investigating physics principles to guide schedule parameters, most clearly-understood theoretical principles do not apply to current, imperfect experimental systems [34]. Hence the empirical approach, which we take in this paper, represents current state-of-the-art [58]. Three degrees of freedom are specifically investigated in this work.

- First, there are many ways of mapping a problem to an equivalent Ising formulation that runs on the machine (we investigate one such mapping in Section 3).
- Second, the user may accelerate or delay \( A(t)/B(t) \) evolution, thus determining *annealing time* \( (1\text{−}300 \text{ μs}) \), the duration of the machine’s computation.
- Finally, the user may introduce stops (*anneal pause*) in the annealing process, which have been shown to improve performance in certain settings [43].

### 3 DESIGN

Starting from the abstract QA problem form (§3.1), QuAMax’s design reduces ML detection to form (§3.2), then compiles it on actual hardware, a process called *embedding* (§3.3).
3.1 QA Problem Formulation

The first step in leveraging QA for any problem is to define the problem of interest as an objective function to be minimized, consisting of a quadratic polynomial of binary variables. We now introduce two equivalent forms of this objective function, as is customary in the QA application literature.

1. Ising spin glass form. In this form the solution variables are traditionally referred to as spins $s_i \in \{+1, -1\}$.

\[
\hat{s}_1, \ldots, \hat{s}_N = \arg \min_{s_1, \ldots, s_N} \left( \sum_{i < j} g_{ij} s_i s_j + \sum_i f_i s_i \right)
\]

where $N$ is the number of spin variables, and $g_{ij}$ and $f_i$ are the Ising model parameters that characterize the problem. The $f_i$ characterize the preference for each spin to be $+1$ or $-1$: positive indicates a preference for $-1$ while negative indicates a preference for $+1$, with the magnitude corresponding to the magnitude of the preference for either state. The $g_{ij}$ capture preference for spins: positive causes the QA to prefer $s_i \neq s_j$, while negative causes the QA to prefer $s_i = s_j$ in its optimization outcome. Analogously to $f_i$, the magnitude of $g_{ij}$ corresponds to the magnitude of its preference.

2. QUBO form. The Quadratic Unconstrained Binary Optimization (QUBO) has solution variables $q_i$ that are classical binary bits (zero-one valued):

\[
\hat{q}_1, \ldots, \hat{q}_N = \arg \min_{q_1, \ldots, q_N} \sum_{i < j} Q_{ij} q_i q_j, \quad (3)
\]

where $N$ is the qubit count and $Q \in \mathbb{R}^{N \times N}$ is upper triangular. The off-diagonal matrix elements $Q_{ij}$ ($i \neq j$) correspond to $g_{ij}$ in Eq. 2, and the diagonal elements correspond to $f_i$.

The two forms are equivalent, their solutions related by:

\[
q_i \leftrightarrow \frac{1}{2}(s_i + 1), \quad (4)
\]

leading to $g_{ij} \leftrightarrow \frac{1}{2}Q_{ij}$ and $f_i \leftrightarrow \frac{1}{2}Q_{ii} + \frac{1}{2}\sum_{k=1}^{i-1} Q_{ik} + \frac{1}{2}\sum_{k=i+1}^{N} Q_{ik}$.

3.2 ML-to-QA Problem Reduction

We now explain our process for transforming the ML detection problem into the QUBO and Ising forms. Since QuAmax also assumes OFDM where the wireless channel is subdivided into multiple flat-fading orthogonal subcarriers [49], this ML-to-QA reduction is required at each subcarrier.

3.2.1 ML-to-QUBO problem reduction. Let’s first consider the transformation of the ML problem into QUBO form—the key idea is to find a variable-to-symbol transform function $T(\cdot)$ that represents the "candidate" vector $v$ in the ML search process (Eq. 1 on p. 2) instead of a number of QUBO solution variables. Specifically, we represent each of the $N$ transmitters' candidate symbols $v_i \in \mathcal{O}$ ($1 \leq i \leq N_t$), with log$_2(|\mathcal{O}|)$ QUBO solution variables, naturally requiring $N = N_t \cdot \log_2(|\mathcal{O}|)$ QUBO solution variables for $N_t$ transmitters, and form these QUBO variables into a vector $q_i$ for each encoder $i$: $q_i = [q_{i(1)} \cdots q_{i(|\mathcal{O}|)}]$. For example, $T$ recasts a $2 \times 2$ QPSK ($|\mathcal{O}| = 4$) problem into a QUBO problem with four solution variables, split into two vectors $q_1 = [q_1 \ q_2]$ and $q_2 = [q_3 \ q_4]$. In general, the transform recasts the ML problem of Eq. 1 into the form

\[
\hat{q}_1, \ldots, \hat{q}_N = \arg \min_{q_1, \ldots, q_N} \| y - H e \|^2, \quad (5)
\]

where $e = [T(q_1), \ldots, T(q_N)]^T$. Then, the resulting $N_q$ vectors $\hat{q}_1, \ldots, \hat{q}_N$ correspond to the N QUBO solution variables, $\hat{q}_1, \ldots, \hat{q}_N$. Continuing our $2 \times 2$ QPSK example, $e = [T(q_1), T(q_2)]^T = [T(q_1, q_2)]$ where $T(q_1), T(q_2)$ correspond to the ML solution $v = [v_1, v_2]^T$ in Eq. 1, the nearest symbol vector around received $y$. The decoded vectors $\hat{q}_1, \hat{q}_2$ correspond to the four decoded QUBO variables $\hat{q}_1, \hat{q}_2, \hat{q}_3, \hat{q}_4$ in Eq. 3. If the transmitter's bit-to-symbol mapping and QuAmax's variable-to-symbol transform are equivalent, then the decoded $\hat{q}_1, \hat{q}_2, \hat{q}_3, \hat{q}_4$ are the directly de-mapped bits, $b$ from the ML solution in Eq. 1.

When transform $T$ is linear the expansion of the norm in Eq. 5 yields a quadratic polynomial objective function, since $q_i^T = q_i$ for any 0 or 1-valued $q_i$. Then the ML problem (Eq. 1) transforms directly into QUBO form (Eqs. 3 and 5). Our task, then, is to find variable-to-symbol linear transform functions $T$ for each of BPSK, QPSK, and 16-QAM.

**Binary modulation.** If the two mobile transmitters send two signals simultaneously, each with one of two possible information symbols, their transmissions can be described with a two-vector of symbols $\vec{v} = [v_1, v_2]^T \in \{(\pm 1), (\pm 1)\}$. This type of data transmission is called binary modulation, of which one popular kind is binary phase shift keying (BPSK). The ML problem applied to the BPSK case where symbols $v_i$ are represented by $v_i = T(q_i) = 2q_i - 1$ thus results in a QUBO form (a detailed derivation can be found in Appendix A).

We next consider higher-order modulations, which send one of $M$ possible information symbols with each channel use (where $M > 2$), resulting in higher communication rates.

**QPSK modulation.** In the case of quadrature phase shift keying (QPSK), each sender transmits one of four possible symbols $v_i \in \{1 \pm 1\}$. Since it can be viewed as a two-dimensional BPSK $v_i = \overline{v}_i$, we represent each possibly-transmitted QPSK information symbol with the linear combination of one QUBO variable, plus the other QUBO variable times the imaginary unit. Transforming $q_{i-1}$ and $q_i$ to $v_i$ and $v_i^Q$ respectively leads to the transform $v_i = T(q_i) = (2q_{i-1} - 1) + j2q_i - 1$.

**Higher-order modulation.** 16 quadrature amplitude modulation (16-QAM) and higher-order modulations increase spectral efficiency, but utilize multiple amplitudes (levels) so require a $T$ that inputs more than one (binary) solution variable per I or Q dimension. First consider a transform $T$ for the simplest multi-level 1-D constellation:

\[
\begin{array}{cccc}
0 & 0 & 0 & 0 \\
1 & 0 & 1 & 0 \\
1 & 1 & 0 & 1 \\
1 & 1 & 1 & 1 \\
\end{array}
\]

$T = 4q_1 + 2q_2 - 3$ maps these bits to the values $-3, -1, +1, +3$. Now to generalize this to 2-D, let the first two arguments of $T$, $q_{4i-1}, q_{4i}$, represent the I part and the next two, $q_{4i+1}, q_{4i}$ represent the Q part. We call this transform, shown in Fig. 2(a), the 16-QAM QuAmax transform. It has the desirable property that it maps solution variables to symbols linearly, viz.

$v_i = T(q_i) = (4q_{4i-3} + 2q_{4i-2} - 3) + j(4q_{4i-1} + 2q_{4i} - 3)$, thus results in a QUBO form.
However, transmitters in practical wireless communication systems use a different bit-to-symbol mapping, the Gray code shown in Fig. 2(d), which minimizes bit errors. This means that the QuAMax receiver’s bit to symbol mapping differs from the sender’s. Thus one further step remains so that we may map the decoded QUBO variables into the correct Gray-coded transmitted bits.

A naïve approach is simply for QuAMax to use the Gray-coded bit-to-symbol mapping as its transform $T$. The Gray-coded mapping results in a one-dimensional 4-PAM constellation assuming bits 00, 01, 11, and 10 are transformed to $-3$, $-1$, $+1$, and $+3$ without loss of generality. The transform $v^f_i = 2(2q_{i-3} - 1) + 2(q_{i-3} - q_{i-2})^2 - 1$ would map between a 4-PAM symbol $v^q_i$ and two QUBO variables $q_{i-3}, q_{i-2}$, but the resulting expansion of the ML norm would yield cubic and quartic terms $q_i q_j q_k q_l$ for $r \neq k \neq l (\neq p)$, requiring quadratization with additional variables to represent the problem in QUBO form [8, 33].

Instead, we retain Gray coding at the transmitter and the QuAMax transform at the receiver. To correct the disparity, we develop a bitwise post-translation that operates on QuAMax-transformed solution output bits at the receiver, translating them back into Gray-coded bits (i.e., moving from Fig. 2(a) to Fig. 2(d)). Starting with the QuAMax transform shown in Figure 2(a), if the second bit $\hat{q}_{i-2}$ of the QUBO solution bits $\hat{q}_{i-3}, \hat{q}_{i-2}, \hat{q}_{i-1}, \hat{q}_i$ is 1, then the translation flips the third bit $\hat{q}_{i-1}$ and the fourth bit $\hat{q}_i$ (e.g. 1100 to 1111), otherwise it does nothing. This can be generalized to $2^n$-QAM ($n \geq 2$) as an operation that flips even numbered columns in the constellation upside down. We term the result $b'$ an intermediate code, shown in Figure 2(b). Next, we apply the differential bit encoding transformation of Figure 2(c) to the intermediate code $b'$ to obtain the Gray-coded bits $\hat{b}$ in Figure 2(d) (e.g. translating 1111 to 1000).

**QuAMax decoding example.** To clarify processing across all stages, here we present a complete QuAMax decoding example. Suppose a client maps a bit string $b_1, b_2, b_3, b_4$ onto $v_1$, one of the Gray-coded 16-QAM symbols in Figure 2(d), and sends $v = [v_1]$ to an AP through wireless channel $H$. The AP receives $y = Hv + n$, the transmitted signal perturbed by AWGN. The steps of QuAMax’s decoding are:

1. Form the ML QUBO equation using $H$, $y$, and $v = [v_1] = [T(q_1)]$, where $T(q_1) = (4q_1 + 2q_2 - 3) + j(4q_3 + 2q_4 - 3)$, a linear transform based on the QuAMax transform in Figure 2(a).
2. Solve the QUBO form of the ML detection problem on the QA machine, resulting an ML-decoded vector $\hat{q}_1$, comprised of QUBO variables $\hat{q}_1, \hat{q}_2, \hat{q}_3, \hat{q}_4$.
3. Apply the above bitwise translation from the decoded QUBO solution output $\hat{q}_1, \hat{q}_2, \hat{q}_3, \hat{q}_4$ to Gray-coded received bits $b_1, b_2, b_3, b_4$ (from Figure 2(a) to Figure 2(d)).

If $b_1, b_2, b_3, b_4 = b_1, b_2, b_3, b_4$, decoding is done successfully, noting that in the case of a symbol error, we preserve the aforementioned advantage of Gray coding.

### 3.2.2 ML-to-Ising problem reduction.** The Ising spin glass form of the ML problem can be obtained by simply transforming the resulting QUBO form (§3.2.1) into the Ising form by Eq. 4. Due to the fact that DW2Q implements an Ising model, QuAMax works by using the following generalized Ising model parameters:

**BPSK modulation.** Given a channel matrix $H$ and vector of received signals $y$, we obtain the following Ising model parameters:

$$ f_i(H, y) = -2 \left( H_{(i,i)} \cdot y^f \right) - 2 \left( H_{(Q,i)} \cdot y^Q \right), $$

$$ g_{ij}(H) = 2 \left( H_{(c,i)} \cdot H_{(c,j)} \right) + 2 \left( H_{(Q,i)} \cdot H_{(Q,j)} \right), $$

where $H_{(c,i)}$ denotes the $i$th column of matrix $H$.

**QPSK modulation.** In the case of QPSK, the following is the resulting Ising parameter $f_i$ for QPSK:

$$ f_i(H, y) = \begin{cases} 
-2 \left( H_{([i/2]^j)} \cdot y^Q \right) + 2 \left( H_{([i/2])} \cdot y^Q \right), & \text{if } i = 2n, \\
-2 \left( H_{([i/2]^j)} \cdot y^Q \right) - 2 \left( H_{([i/2])} \cdot y^Q \right), & \text{otherwise}, 
\end{cases} $$

Since the real and imaginary terms of each symbol are independent, the coupler strength between $s_{2n-1}$ and $s_{2n}$ (or $q_{2n-1}$ and $q_{2n}$) is 0. For other $s_i$ and $s_j$, the Ising coupler strength for QPSK is:

$$ g_{ij}(H) = \begin{cases} 
2 \left( H_{([i/2]^j)} \cdot H_{([j/2])} \right) + 2 \left( H_{([i/2])} \cdot H_{([j/2])} \right), & \text{if } i + j = 2n, \\
\pm 2 \left( H_{([i/2]^j)} \cdot H_{([j/2])} \right) \pm 2 \left( H_{([i/2])} \cdot H_{([j/2])} \right), & \text{otherwise}, 
\end{cases} $$

where $i < j$ and the sign of the latter case of Eq. 8 is determined by whether $i = 2n$ (when $i = 2n$, then ‘+’ and ‘−’).
In summary, the process to obtain the Ising spin glass form can be simplified with these generalized Ising model parameters; a QuA-Max system simply inserts the given channel H and received signal y at the receiver into these generalized forms accordingly, not requiring any computationally expensive operations (i.e. directly considering the expansion of the norm in Eq. 5). Thus, computational time and resources required for ML-to-QA problem conversion are insignificant and can be neglected.

Table 2: Logical (physical) number of qubits required for various configurations of the elementary adiabatic quantum ML decoder. For each configuration, bold font indicates non-feasibility on the current (2,031 physical qubit) D-Wave machine with Chimera connectivity.

<table>
<thead>
<tr>
<th>Config.</th>
<th>BPSK</th>
<th>QPSK</th>
<th>16-QAM</th>
<th>64-QAM</th>
</tr>
</thead>
<tbody>
<tr>
<td>10 × 10</td>
<td>10 (40)</td>
<td>20 (120)</td>
<td>40 (440)</td>
<td>60 (1K)</td>
</tr>
<tr>
<td>20 × 20</td>
<td>20 (120)</td>
<td>40 (440)</td>
<td>80 (2K)</td>
<td>120 (4K)</td>
</tr>
<tr>
<td>40 × 40</td>
<td>40 (440)</td>
<td>80 (2K)</td>
<td>160 (7K)</td>
<td>240 (15K)</td>
</tr>
<tr>
<td>60 × 60</td>
<td>60 (1K)</td>
<td>120 (4K)</td>
<td>240 (15K)</td>
<td>360 (33K)</td>
</tr>
</tbody>
</table>

3.3 Embedding into QA hardware

Once the ML detection problem is in quadratic form, we still have to compile the corresponding Ising model onto actual QA hardware. The D-Wave machine works by implementing an Ising model objective function energetically hardcoded into the chip, so the problem (Eq. 2 on p. 4) can support a certain coefficient $g_{ij}$ to be non-zero only if variables $s_i$ and $s_j$ are associated to physical variables (qubits or physical qubits) located on the chip in such a way that the qubits are energetically coupled. In the case of the DW2Q machine we use the coupling matrix is a Chimera graph, shown in Figure 3(a), with each node corresponding to a qubit. Once Ising coefficients are passed to the annealer, the hardware assigns them to the edges of the Chimera graph, which are divided (along with their connected nodes) into unit cells. Note however, that the Ising problem generated from Eq. 1 is almost fully connected (i.e., $g_{ij} \neq 0$ for most $(i, j)$ pairs), the Chimera graph itself has far from full connectivity, and so a process of embedding the Ising problem into the Chimera graph is required.

One standard method of embedding is to “clone” variables in such a way that a binary variable becomes associated not to a single qubit but to a connected linear chain of qubits instead: a logical qubit, as shown in Figure 3(b).3 We show an embedding of a fully-connected graph of 12 nodes. Each unit cell on the diagonal holds four logical qubits (a chain of two qubits), while the other unit cells are employed in order to inter-connect the diagonal cells. Specifically, suppose unit cell $[1, 1]$ includes logical qubits 1–4 and unit cell $[2, 2]$ includes logical qubits 5–8. The left side of unit cell $[2, 1]$ has a vertical clone of qubits 5–8 and the right side has a horizontal clone of logical qubits 1–4. Then, logical qubits 1–4 and 5–8 are all connected by means of the single unit cell $[2, 1]$. The unit cell hosting the next four logical qubits 9–12 is placed at coordinates $[3, 3]$. Two unit cells below, $[3, 1]$ and $[3, 2]$, are used for connections between 9–12 and 1–4, and 9–12 and 5–8 respectively.

Given a number $N$ of spin variables (i.e., logical qubits) in Ising form, this embedding represents each with a chain of $\lceil N/4 \rceil + 1$ qubits, for a total of $N \lceil N/4 \rceil + 1$ qubits. Recall that $N = N_t \cdot \log_2(\Theta)$. Table 2 summarizes the size of the embedding in both logical and physical qubits, as a function of the MIMO detection problem’s parameters—number of users and AP antennas, and modulation type. Color coding and bold font indicate whether or not the given parameters fit into the number of qubits available on current D-Wave machines.

The embedded version of the Ising problem. After embedding into Chimera graph we need to recast the Ising problem into an equivalent problem that has the same ground state, but also satisfies the Chimera graph constraints. We also need to introduce a constant penalty term ($J_F$) to quantify the relatively large coupling that constrains all physical qubits belonging to the same logical qubit to prefer the same state. Appendix B contains additional detail, but we discuss important experimental considerations for choosing $J_F$ in Section 5.3.

Unembedding with majority voting. The bit string that the DW2Q returns is expressed in terms of the embedded Ising problem, and so must be unembedded in order to have the values of the bits expressed in terms of our ML Ising problem. This is done by checking that all the qubits of a logical chain are either +1 or −1. Should not all spins be concordant, the value of the corresponding logical variable is obtained by majority voting (in case of a vote tie, the value is randomized). Once the logical variables are determined, each configuration yields the corresponding energy of the Ising objective function by substituting it into the original Ising spin glass equation (Eq. 2).

4 IMPLEMENTATION

This section describes our implementation on the D-Wave 2000Q quantum annealer (DW2Q), explaining the API between the annealer’s control plane and its quantum substrate, machine parameters, and their tuning to the problem at hand.

Figure 3: A comparison between the quantum hardware graph of the used machine (which misses some nodes due to manufacturing defect), and the topology of our elementary quantum ML hardware graph before embedding into the hardware graph.
Each anneal cycle on the DW2Q yields a configuration of spins (i.e., one decoded bit string). The user programs the annealer to run a batch of $N_a$ annealing cycles (one QA run) with the same parameters to accumulate statistics, which means that we have a set of $N_a$ configurations from a DW2Q job submission. The lowest energy configuration among $N_a$ anneals is the best answer found.

**Parallelization.** Multiple instances (identical or not) can be run physically alongside each other, reducing run time by the parallelization factor

$$P_F = N_{tot}/(N\left\lfloor N/4 \right\rfloor + 1)$$

—a small 16-qubit problem employing just 80 physical qubits (e.g., 16-user BPSK, 8-user QPSK, and 4-user 16-QAM) could in fact be run more than 20 times in parallel on the DW2Q.

**Precision Issues.** As analog devices, the desired embedded Ising coefficients (Eqs. 10-12 in Appendix B) do not perfectly match their real energy values once hardcoded in the real machine, and hence give rise to intrinsic control errors (ICE), an uncontrollable shift in the actual programmed values of the objective function. ICE is appropriately modeled as a noise fluctuating at a time scale of the order of the anneal time, i.e., on each anneal, Ising coefficients are perturbed: $f_i \rightarrow f_i + (\delta f_i), g_{ij} \rightarrow g_{ij} + (\delta g_{ij})$, where the noise is Gaussian with mean and variance measured $(\delta f_i) \approx 0.008 \pm 0.02$ and $(\delta g_{ij}) \approx -0.015 \pm 0.025$ in the most delicate phase of the annealing run [16]. The impact of ICE on performance depends on the problem at hand [12, 78], but it is clear that precision issues will arise if the largest energy scale squeezes the value of the coefficients (in Eqs. 11–12 in Appendix B) to a level where ICE is likely to erase significant information of the problem’s ground state configuration.

**Annealer Parameter Setting.** As discussed in Section 3.3, the $|J_F|$ that enforces a chain of qubits to return a series of values which are all in agreement (either all +1 or −1), and the annealing time $T_a$ are both key performance parameters that determine the net time to find a solution, and hence overall QA performance. We also introduce 1, 10, and 100 µs pause time $T_p$ in the middle of annealing ($T_a = 1 \mu$s) with various pause positions $s_p$, to see the effect of pausing [43] on our problems. Setting $|J_F|$ too large would wash out the problem information due to ICE, however $|J_F|$ on average should increase with the number of logical chains in fully-connected problems in the absence of ICE [69]. Due to the lack of a first-principles predictive theory on the correct value for a given instance, we present in Section 5.3 an empirical investigation of the best embedding parameters, employing the microbenchmarking methodologies generally accepted [52, 57, 69]. Below we perform a sensitivity analysis on $|J_F|$, $T_a$, $T_p$, and $s_p$ (§5.3.1) over the ranges $|J_F| \in \{1.0 - 10.0 (0.5)\}$, $T_a \in \{1, 10, 100 \mu s\}$, $T_p \in \{1, 10, 100 \mu s\}$, and $s_p \in \{0.15 - 0.55 (0.02)\}$.

**Improved coupling dynamic range.** The dynamic range of coupler strengths is defined as the ratio between the maximum and minimum values that can be set $(g_{ij}$ in Eq. 2). To strengthen interactions between embedded qubits, the DW2Q is able to double the magnitude of valid negative coupler values, effectively increasing the precision of embedded problems and reducing ICE. However, this improved range option, when enabled, breaks the symmetry of the Ising objective function (substituting the opposite signs for connected coefficients and their couplings, into the same problem), and hence precludes averaging over these symmetrical instances as the DW2Q does without the improved range option, to mitigate leakage errors [4]. It is thus unclear whether the use of this feature is beneficial in the end without experimentation, and so we benchmark in Section 5 both with and without improved range.

5 EVALUATION

We evaluate QuAMax on the DW2Q Quantum Annealer machine shown in Figure 1. We consider the same number of antennas at the clients and AP (i.e., $N_t = N_r$). Section 5.1 introduces QA results, while Section 5.2 explains our experimental methodology. After that in Section 5.3 we present results under only the presence of the annealer’s internal thermal noise (ICE). Sections 5.4 and 5.5 add wireless AWGN channel noise and trace-based real-world wireless channels, respectively, quantifying their interactions with ICE on end-to-end performance. Over $8 \times 10^{10}$ anneals are used in our performance evaluation.

5.1 Understanding Empirical QA Results

We begin with a close look at two runs of the QA machine, to clarify the relationships between Ising energy, Ising energy-ranked solution order, and BER. Figure 4 shows six QA problem instances (all of which require 36 logical qubits), corresponding to two different wireless channel uses for each of varying modulation and number of users. The solutions are sorted (ranked) by their relative Ising energy difference $\Delta E$ from the minimum Ising energy (blue numbers
atop selected solutions), where red bars show each solution’s frequency of occurrence (in the rare case of two or more tied distinct solutions, we split those solutions into multiple solution ranks). The number of bit errors associated with each solution appears as a green curve. For statistical significance, this data summarizes 50,000 anneals, more than QuAMax’s practical operation. As modulation order increases and number of users decreases (from left to right in Figure 4), the probability of finding the ground state tends to be lower, while the search space size remains constant, leading eventually to higher BER and FER. The relative Ising energy gap also trends smaller, and is likely to be inversely correlated with the impact of ICE on the problem instance [2, 78].

5.2 Experimental methodology
In this section, we introduce performance metrics and figures of merit that give insight into the operation of the QA machine as it solves the ML MIMO decoding problem.

We note that in our performance evaluation we exclude from consideration programming time and post-programming time of the Ising coefficients on the chip, and readout latency of the qubit states after a single anneal. Currently, these times dominate the pure computation time (i.e. total anneal time) by several orders of magnitude (milliseconds), due to engineering limitations of the technology. However, these overheads do not scale with problem size and are not fundamental performance factors of the fully integrated QuAMax system, and so this is in accordance with experimental QA literature convention. We discuss these overheads in Section 7.

5.2.1 Metric: Time-to-Solution (TTS). Suppose we find the ground state (corresponding to the minimum energy solution within the search space of $2^N$ bit strings, where $N$ is the variable count) with probability $P_0$. In the absence (but not presence) of channel noise, this ground state corresponds to a correct decoding. Each anneal is an independent, identically-distributed random process, meaning that the expected time to solution, or $TTS(P)$, is the anneal time of each anneal $T_a$ multiplied by the expected number of samples to be able to find the ML solution with probability $P$: $TTS(P) = T_a \cdot \log(1 - P)/\log(1 - P_0)$. TTS is commonly used in the QA literature setting $P = 0.99$ [58].

5.2.2 Our Metrics: BER and Time-to-BER (TTB). TTS reflects the expected time to find the ground state, but does not characterize the expected time our system takes to achieve a certain Bit Error Rate (BER, averaged across users), the figure of merit at the physical layer. This quantity differs from TTS, because TTS only considers the ground state, and as illustrated in the example shown in Figure 4, solutions with energy greater than the ground state may also have (rarely) no or relatively few bit errors, while wireless channel noise may induce bit errors in the ground state solution itself. Hence we introduce a metric to characterize the time required to obtain a certain BER $p$, Time-to-BER: $TTB(p)$. This is preferred in our setting, since a low but non-zero bit error rate is acceptable (error control coding operates above MIMO detection).

TTB for a single channel use. Since one QA run includes multiple ($N_a$) anneals, we return the annealing solution with minimum energy among all anneals in that run. We show an example of this process for one instance (i.e., channel use, comprised of certain transmitted bits and a certain wireless channel) in Fig. 4. The annealer finds different solutions, with different Ising energies, ranking them in order of their energy. Considering this order statistic, and the fact that QuAMax considers only the best solution found by all the transmitted bits and a certain wireless channel, the expected BER of instance $I$ after $N_a$ anneals can be expressed as

$$ \mathbb{E}(BER(N_a)) = \sum_{k=1}^{L} \left( \sum_{r=k}^{L} p(r) \right) N_a - \left( \sum_{r=k+1}^{L} p(r) \right) N_a \cdot F_I(k)/N, \quad (9) $$

where $N$ is qubit count, $L \leq N_a$ is the number of distinct solutions, $r (1 \leq r \leq L)$ is the rank index of each solution, $p(r)$ is the probability of obtaining the $r$th solution, and $F_I(k)$ is the number of bit errors of the $k$th solution against ground truth. To calculate $TTB(p)$, we replace the left hand side of Eq. 9 with $p$, solve for $N_a$, and compute $TTB(p) = N_a T_a / p_f$.

Generalizing to multiple channel uses. The preceding predicts TTB for a fixed instance. In the following study we compute TTB and BER across multiple instances (random transmitted bits and randomly-selected wireless channel), reporting statistics on the resulting sampled distributions.

5.3 Performance Under Annealer Noise
This section presents results from the DW2Q annealer for wireless channel noise-free scenarios, in order to characterize the machine’s performance itself as a function of time spent computing. Sections 5.4 and 5.5 experiment with Gaussian noise and trace-based wireless channels, respectively.

In this section, we run several instances with unit fixed channel gain and average transmitted power. Each instance has a random-phase channel, randomly chosen transmitted bit string, and is repeated for each of three different modulations (BPSK, QPSK, 16-QAM) and varying numbers of users and AP antennas. Each instance is reduced to Ising as described in Section 3.2, for a total of 780 different problems per QA parameter setting. Unless otherwise specified, this and subsequent sections use the fixed parameter settings defined in §5.3.1. We obtain significant statistics by post-processing up to 50,000 anneals per QA run (except 10,000 anneals for QPSK as described in Figure 7).

5.3.1 Choosing Annealer Parameters. In order to isolate the effect of different parameter settings on individual problems, we employ microbenchmarks on TTS. This section explains our choice of parameter settings for our main performance results in §5.3.3, §5.4, and §5.5. Note that while we plot results here only for BPSK and QPSK to save space, our results show that the methods, arguments and observations generalize to higher modulations, unless otherwise indicated. For the purpose of setting the parameters, we restrict the dataset to the ML problems that solve within a median TTS(0.99) of 10 ms for which we have low uncertainty on the measured success probability. We use the determined parameters for all instances regardless of their TTS for the performance analysis.

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5 See section 5.2.2. Frame error rate FER is computed as $1 - (1 - BER) \cdot \text{frame size}$.

6 The energy distribution of the Ising objective function (Eq. 2) corresponds to the distribution of ML decoder Euclidean distances (Eq. 1).
Annealer Parameter Optimization. Based on the previous sensitivity analysis, we select a default QA parameter setting. First, we choose improved dynamic range since it is relatively robust to choice of $|J_F|$, nearly equaling the best performance of the standard dynamic range. Second, we choose $T_p = 1 \mu s$, since it shows better results and greater pause times dominate the anneal time.

5.3.2 Choosing whether to pause. With the above default QA parameters, we now use TTB to explore whether or not we should use the QA pause functionality, as TTB encompasses both algorithms’ BER performance as well as wall clock running time (cf. TTS). We first define a fixed parameter setting by selecting the best estimated choices for the non-pausing algorithm and for the pausing algorithm, meaning the parameters which optimize medians across a sample of instances belonging to the same problem class (e.g. 18×18 QPSK). This approach is to be compared against an oracle that optimizes $|J_F|$, $T_a$ or $|J_F|$, $s_p$ instance by instance. In the figures, we denote the two parameter setting methods as Fix (fixed) and Opt (optimal), respectively.

Our motivation for considering Opt is that it provides a bound to what can be achieved by the methods that seek to optimize machine parameter settings instance by instance [68, 70], currently under investigation. With our traces we compute BER as a function of $N_a$ using Eq. 9; the median result across 20 random instances is shown in Figure 8 (upper). Figure 8 (lower) shows the corresponding BER as a function of time (i.e., TTB). Note that the pausing algorithm has a better performance than the non-pausing algorithm (regardless of Opt and Fix strategy) despite the fact that each anneal in the former ($T_a + T_p$) takes twice as much time than the latter (when $T_a = 1 \mu s$). Based on this empirical finding, we will present the results in the following section only for the protocol that includes a pause.
5.3.3 QuAMax: End-to-End Performance. We now evaluate the TTB and TTF (Time-to-FER) of QuAMax, comparing:

1. **QuAMax**: Fixed-parameter, average-case performance.
2. **Oracle**: Median-case Opt performance (§5.3.2: outlier data points have minimal influence on the median order statistic), optimizing QA parameters.\(^8\)

Figure 9 shows the TTB with varying user numbers and modulations at the edge of QuAMax’s performance capabilities. Solid and dashed lines report median and average BER, respectively. We note that mean TTB dominates median TTB due to a small number of long-running outliers. QuAMax accordingly sets a time deadline (measured median TTB for the target BER) for decoding and after that discards bits, relying on forward error correction to drive BER down. Next considering the relationship between TTB and problem size, Fig. 10 explores TTB for target BER \(\leq 10^{-6}\), for each instance that reaches a BER of \(10^{-6}\) within 10 ms as well as average performance. ML problems of these sizes are well beyond the capability of conventional decoders (cf. Table 1), and we observe that Opt achieves superior BER within 1–100 \(\mu s\) and that QuAMax achieves an acceptable BER for use below error control coding. Note that instances with TTB below the minimum required time (i.e., \(T_a + T_p\)) caused by parallelization require (an amortized) 2 \(\mu s\).

Next, we consider frame error rate performance, measuring mean and median FER QuAMax achieves. Results in Fig. 11 show that tens of microseconds suffice to achieve a low enough (below \(10^{-3}\)) FER to support high throughput communication for 60-user BPSK, 18-user QPSK, or four-user 16-QAM suffices to serve four users with the idealized median performance of Opt. QuAMax (mean Fix) achieves a similar performance with slightly smaller numbers of users. Furthermore, our results show low sensitivity to frame size, considering maximal-sized internet data frames (1,500 bytes) all the way down to TCP ACK-sized data frames (50 bytes).

5.4 Performance under AWGN Noise

We next evaluate the impact of AWGN from the wireless channel, testing six SNRs ranging from 10 dB to 40 dB. In order to isolate the effect of noise, the results in this subsection fix the channel and transmitted bit-string and consider ten AWGN noise instances. Looking at the data in depth to begin with, the effect of AWGN channel noise, which is itself additive to ICE, is shown in Fig. 12 for six illustrative examples. As SNR increases, the probability of finding the ground state and the relative energy gap tend to increase. At 10 dB SNR the energy gap between the lowest and second lowest energy solutions narrows to just three percent, leaving minimal room for error. In terms of overall performance, Fig. 13 (left) shows TTB at 20 dB SNR, varying number of users and modulation. At a fixed SNR, we observe a graceful degradation in TTB as the number of users increases, across all modulations. Fig. 13 (right) shows TTB at a certain user number, varying SNR and modulation. At a fixed user number, as SNR increases, performance improves, noting that the idealized median performance of Opt shows little sensitivity to SNR, achieving \(10^{-6}\) BER within 100 \(\mu s\) in all cases.
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Figure 13: TTB comparison across different user numbers, modulations, and SNRs. Left: varying the number of users at SNR 20 dB. Right: varying SNR at a certain number of users. Thick lines report QuAMax’s performance (mean Fix), and same style but thin (purple) lines report the idealized performance (median Opt).

Figure 14: QuAMax’s performance comparison against the zero-forcing decoder across different user numbers, modulations, and SNRs. Each × symbol (left-to-right: 36, 48, 60 users for BPSK and 12, 14, 16 users for QPSK) reports the zero-forcing decoder’s BER and corresponding processing time.

Fig. 14 compares QuAMax’s performance versus zero-forcing decoder at bad SNR scenarios, showing the necessity of ML-based MIMO decoders for large MIMO system. Linear decoders such as zero-forcing and MMSE suffer from the effect of the poor channel condition (when \( N_t \approx N_r \)), requiring \( N_r > N_t \) (i.e., more antennas) for appropriate BER performance. In Figure 14, QuAMax reaches the zero-forcing’s BER (or even better BER) approximately 10-1000 times faster than zero-forcing in both BPSK and QPSK modulation. Here, computation times for zero-forcing are inferred from processing time using a single core in BigStation [76], one of the current large MIMO designs based on zero-forcing. While this processing time can be reduced proportionally with more cores, BER (i.e., quality of solutions) remains unchanged. The Sphere Decoder achieves comparable BER, but processing time cannot fall below a few hundreds of \( \mu s \) with the given numbers of users and SNRs.\(^9\)

Extreme levels of parallelization or GPU implementation might be able to resolve the issue. However, practical constraints will eventually limit the increase in performance on classical platforms [38]. Contrarily, overheads in QuAMax are apart from pure computation, which can be resolved by engineering design.

5.5 Trace-Driven Channel Performance

We evaluate system performance with real wideband MIMO channel traces at 2.4 GHz, between 96 base station antennas and eight static users [61]. This dataset comprises the largest MIMO trace size currently available. For each channel use, we randomly pick eight base station antennas to evaluate the \( 8 \times 8 \) MIMO channel use at SNR ca. 25–35 dB. Fig. 15 shows the resulting TTB and TTF. We achieve \( 10^{-6} \) BER and \( 10^{-4} \) FER within 10 \( \mu s \) for QPSK. For BPSK, considering multiple problem instances operating in parallel, we achieve the same BER and FER within (an amortized) 2 \( \mu s \) period. This implies that tens of microseconds suffice to achieve a low BER and FER even without parallelization of identical problems, which creates an opportunity for QuAMax to parallelize different problems (e.g., different subcarriers’ ML decoding).

6 RELATED WORK

Applications of QA. Despite the immaturity of software toolchains, existing quantum annealing machines have been already programmed successfully to solve problems in Planning and Scheduling [57], Databases [66], Fault Diagnostics [55], Machine Learning [54], Finance [59], Data Analysis [47], Chemistry [31], and Space Sciences/Aeronautics [3]. A similar problem to ML detection, CDMA multiuser demodulation, was solved using quantum fluctuations controlled by the transverse field (similar as QA) in [53]. Of particular relevance is work on optimization of fully-connected graphs, such as the ones used to map the ML problem [69]; the results of which showed that QA performance could match the most highly optimized simulated annealing code run on the latest Intel processors. For further details on the logical to physical qubit embedding process, see Venturelli et al. [69]. Efficient embeddings which do not force the chip coverage to be a triangle are also known [7].

QAOA. Quantum Approximate Optimization Algorithms, invented in 2014 [23], and recently generalized for constrained combinatorial optimization [28], require digital gate-model QC, which became available at reasonable scale only in 2017 (prototypes from IBM, Rigetti Computing, and Google are available). While QA and QAOA require different hardware (the former is analog, the latter digital) they have in common that: (1) For problems that don’t have hard
constraints, the programming step consists in defining a classical combinatorial problem which is cast into QUBO [9, 72] or Ising form, hence they both may leverage our formulation §3.2. (2) QAOA can be seen in some parameter range as a “digitized” version of QA, and it has been formally demonstrated that it can simulate the results and performance of QA and outperform it, in principle [77]. The first commonality is particularly important since it opens the door to application of our techniques on future hardware capable of running QAOA.

Conventional ML Detectors. Faster silicon based ML detector strategies typically approximate and parallelize the ML computation [15, 73]. In these general directions, much progress has been made to the point that Sphere Decoders have been realized in ASIC hardware [10, 74] but fall short for the reasons noted in Table 1 when the setting demands more antennas at the AP (serving more users), or when the modulation chosen increases [32, 76].

7 DISCUSSION

In this section, we discuss the current status of QA technology and practical considerations.

Computational Power Consumption. The computation in the DWQ2 is performed at zero energy consumption, as dictated by reversible computing, although energy is dissipated in the initialization and readout. The DWQ2 draws 16 kW of power, primarily used by the cryogenic refrigeration unit [17]. The computational power (per watt) for QPUs is expected to increase much more rapidly than for conventional computing platforms since the DWQ2 power draw is not expected to change much as qubit and coupler counts grow in future generation systems while the computational power substantially increases.

Operating Expenses. Operating the DWQ2 results in significant electricity cost, and the dilution refrigerator requires liquid nitrogen 1-2 times a month, for a total yearly cost of about USD $17,000.

Processing Times. The scenario envisioned by QuAMax assumes a centralized RAN architecture where a QPU, co-located with centralized RAN computational resources in a data center, is connected to the APs via high-speed fiber or millimeter-wave links. In this setting, a latency between the APs and data center will not be significant. Nonetheless, QuAMax cannot be deployed today, since additional processing times in the current QPU include approximately 30-50 ms preprocessing time, 6-8 ms programming time, and 0.125 ms readout time per anneal. These overheads are well beyond the processing time available for wireless technologies (at most 3–10 ms). However, these overhead times are not of a fundamental nature and can be reduced by several orders of magnitude by efforts in system integration. By means of extrapolation of improvement trends it is expected that quantum engineering advances in superconducting qubit technology will enable QuAMax to be viable within a decade. Moreover, QuAMax’s Ising form (in Section 3.2.2) can be adapted to be run in other emerging physics-based optimization devices based on photonic technologies [29] whose processing times overhead are in principle much faster. Hence, we leave an end-to-end evaluation in a fully centralized RAN architecture, with more advanced hardware, as future work.

8 CONCLUSION

QuAMax is the first design, implementation and experimental evaluation of a quantum-computing solver for the computationally challenging ML MIMO decoding problem. Our performance results establish a baseline for a future fully-integrated systems in the context of the centralized RAN architecture. We show that once engineering efforts optimize the integration between quantum and conventional computation, quantum computation should be considered a competitive technology for the future design of high-capacity wireless networks.

Future Work. There are several improvements over the design we have evaluated here. First, we anticipate that further optimization of $|J_F|$, $T_a$, and $s_p$ as well as new QA techniques such as reverse annealing [68] may close the gap to Opt performance. Second, there are changes in QA architecture expected in annealers due this year [21] featuring qubits with $2\times$ the degree of Chimera, $2\times$ the number of qubits and with longer range couplings. Based on similar gains in recent results on different problem domains [29], we anticipate this will permit ML problems of size, e.g. $175 \times 175$ for QPSK and dramatically increase the parallelization opportunity of the chip due to the reduced embedding overhead where each chain now only requires $N/12 + 1$ qubits.

Going forward, we will benefit from QA technology improvements from the international community manufacturing quantum annealers with advanced capabilities. According to the development roadmap for these next-generation quantum optimizers, it is expected that in ca. a decade a system such as QuAMax could be based on chips with tens of thousands of highly-connected qubits, with annealing schedules capable of more advanced quantum effects (e.g. non-stoquasticity [51]) and engineering advances will have order-of-magnitude improvements on the aforementioned overhead operation times. While quantum annealers are ahead in terms of number of qubits, gate-model systems offer additional controls that may conceivably increase performance in the future. We will investigate MIMO ML decoding on gate-model QPUs in future work, which currently cannot support algorithms that decode more than $4 \times 4$ BPSK.

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REFERENCES


Appendices are supporting material that has not been peer reviewed.
B EMBEDDED ISING

Embedding maps the Ising problem to an equivalent one that has the same ground state, but also satisfies Chimera graph constraints. The QuAMax compiled objective function is:

\[ F^\text{Case}(\mathbf{H}) = -\frac{N}{2} \sum_{i=1}^{N} s_i s_{i+1} + \sum_{i=1}^{N} \frac{f_i}{|J_i|} \left( \sum_{c=1}^{[N/4]+1} s_i c - s_{i+1} c \right) + \sum_{i,j=1}^{N} \frac{g_{ij}}{|J_{ij}|} s_i c_j \]

where the original logical variables \( s_c \) are now associated to a chain \( i = 1 \ldots ([N/4]+1) \) qubits, indexed with new spins \( s_{ij} \). \(|J_i|\) penalizes the condition that \( s_{ij} \neq s_{ij+1} \), i.e., enforces that all qubits in the chain assume the same value (±1). This enforcement is more likely to happen for large values of \(|J_i|\), however the maximum negative energy value is set to −1 by hardware design. In (11) and (12), \(|J_i|\) effectively renormalizes all terms in the objective function by the factor \(|J_i|^{-1}\). The linear term value \( f_i \) is additionally divided by the number of qubits in a chain \([N/4]+1\). The term in (12) shows that the duplication of variables ensures the existence of a pair of qubits in the chains such that a physical coupler in the Chimera graph exists (\( \delta_{ij} \) is the set of pairs of qubits that are connected by a physical bond once the chains \( i \) and \( j \) are specified).

C 16-QAM ISING MODEL PARAMETERS

Following are the Ising parameters \( f_i \) for 16-QAM:

\[ f_i(H, y) = \begin{cases} 
\text{case } i = 4n - 3 : 
-4 \left( H_{1,(i/4), y}^Q \right) 
\text{case } i = 4n - 2 : 
-2 \left( H_{1,(i/4), y}^Q \right) 
\text{case } i = 4n - 1 : 
-4 \left( H_{1,(i/4), y}^Q \right) 
\text{case } i = 4n : 
-2 \left( H_{1,(i/4), y}^Q \right) 
\end{cases} \]

Since real and imaginary terms of each symbol are independent, the coupler strength between \( s_{4n-3}, s_{4n-2} \) and \( s_{4n-1}, s_{4n} \) is 0. For other \( s_i \) and \( s_j \), the Ising coupler strength \( g_{ij} \) for 16-QAM is:

\[ g_{ij}(H) = \begin{cases} 
\text{case } i = 4n - 3 : 
8 \left( H_{1,(i/4), y}^Q \right) 
\text{case } i = 4n - 2 : 
4 \left( H_{1,(i/4), y}^Q \right) 
\text{case } i = 4n - 1 : 
-8 \left( H_{1,(i/4), y}^Q \right) 
\text{case } i = 4n : 
-4 \left( H_{1,(i/4), y}^Q \right) 
\end{cases} \]